

**CBSE Test Paper 04**  
**Chapter 1 Real Numbers**

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1. The largest number which divides 245 and 1029 leaving remainder 5 in each case is **(1)**
  - a. 8
  - b. 12
  - c. 4
  - d. 16
2. Every positive odd integer is of the form \_\_\_\_\_ where 'q' is some integer. **(1)**
  - a.  $2q + 2$
  - b.  $5q + 1$
  - c.  $3q + 1$
  - d.  $2q + 1$
3. Which of the following is a rational number?  $\sqrt{15}$ ,  $\sqrt{9}$ ,  $\sqrt{10}$ ,  $\sqrt{12}$ . **(1)**
  - a.  $\sqrt{12}$
  - b.  $\sqrt{9}$
  - c.  $\sqrt{10}$
  - d.  $\sqrt{15}$
4. What is a lemma? **(1)**
  - a. contradictory statement
  - b. proven statement
  - c. no statement
  - d. None of these
5. If  $\text{HCF}(a, b) = 12$  and  $a \times b = 1800$ , then  $\text{LCM}(a, b)$  is **(1)**
  - a. 150
  - b. 90
  - c. 900
  - d. 1800
6. The HCF of two numbers is 145 and their LCM is 2175. If one number is 725, find the other. **(1)**

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7. What is the HCF of the smallest composite number and the smallest prime number? **(1)**
  8. Find the HCF of the following polynomials:  $x^8 - y^8$ ;  $(x^4 - y^4)(x + y)$ . **(1)**
  9. An army contingent of 1000 members is to march behind an army band of 56 members in a parade. The two groups are to march in the same number of columns. What is the maximum number of columns in which they can march? **(1)**
  10. If a and b are prime numbers, then what is their L.C.M.? **(1)**
  11. Find the HCF of 1,656 and 4,025 by Euclid's division algorithm. **(2)**
  12. Find the smallest number which when increased by 17 is exactly divisible by both 520 and 468. **(2)**
  13. Write a rational number between  $\sqrt{2}$  and  $\sqrt{3}$ . **(2)**
  14. If p is a prime number, then prove  $\sqrt{p}$  that is an irrational. **(3)**
  15. Find the HCF of 180, 252 and 324 by using Euclid's division lemma. **(3)**
  16. Prove that  $15 + 17\sqrt{3}$  is an irrational number. **(3)**
  17. Find the LCM and HCF of 336 and 54 and verify that  $\text{LCM} \times \text{HCF} = \text{product of two numbers}$ . **(3)**
  18. On dividing the polynomial  $4x^4 - 5x^3 - 39x^2 - 46x - 2$  by the polynomial  $g(x)$ , the quotient is  $x^2 - 3x - 5$  and the remainder is  $-5x + 8$ . Find the polynomial  $g(x)$ . **(4)**
  19. If the HCF of 152 and 272 is expressible in the form  $272 \times 8 + 152x$ , then find x. **(4)**
  20. Prove that if x and y are odd positive integers, then  $x^2 + y^2$  is even but not divisible by 4. **(4)**

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**Solution**

1. d. 16

**Explanation:** Let us subtract 5 (the remainder) from each number in order to find their HCF.

$$245 - 5 = 240$$

$$1029 - 5 = 1024$$

Now, Let us find HCF of 240 , 1024

$$1024 = 240 \times 4 + 64$$

$$240 = 64 \times 3 + 48$$

$$64 = 48 \times 1 + 16$$

$$48 = 16 \times 3 + 0$$

The largest number which divides 245 and 1029 leaving remainder 5 in each case is 16.

2. d.  $2q + 1$

**Explanation:** Let  $a$  be any positive integer and  $b = 2$

Then by applying Euclid's Division Lemma,

we have,  $a = 2q + r$ ,

where  $0 \leq r < 2 \Rightarrow r = 0$  or  $1 \therefore a = 2q$  or  $2q + 1$ .

Therefore, it is clear that  $a = 2q$  i.e.,  $a$  is an even integer.

Also,  $2q$  and  $2q + 1$  are two consecutive integers, therefore,  $2q + 1$  is an odd integer.

3. b.  $\sqrt{9}$

**Explanation:**  $\sqrt{9}$  is an irrational number but because  $\sqrt{9} = \sqrt{3^2} = 3$  and 3 is a rational number.

4. b. proven statement

**Explanation:** A lemma is a proven statement that is used to prove another statement.

5. a. 150

**Explanation:** Using the result,

$HCF \times LCM = \text{Product of two natural numbers}$

$$\Rightarrow LCM(a, b) = \frac{1800}{12} = 150$$

6. We are given that:

$$HCF = 145, LCM = 2175 \quad a = 725 \text{ and } b = ?$$

We know that

$$LCM \times HCF = a \times b$$

$$b = \frac{HCF \times LCM}{a}$$
$$= \frac{145 \times 2175}{725} = 435$$

Therefore the second number is 435

7. The smallest prime number is 2 and the smallest composite number is  $4 = 2^2$

Hence the required HCF  $(4, 2) = 2$

8.  $P(x) = x^8 - y^8$

$$= (x - y)(x + y)(x^2 + y^2)(x^4 + y^4) \text{ Using Identity } a^2 - b^2 = (a + b)(a - b)$$

$$Q(x) = (x^4 - y^4)(x + y)$$

$$= (x - y)(x + y)(x^2 + y^2)(x + y) \text{ Using Identity } a^2 - b^2 = (a + b)(a - b)$$

$$\therefore HCF = (x - y)(x + y)(x^2 + y^2) = x^4 - y^4$$

$$\text{Using Identity } a^2 - b^2 = (a + b)(a - b)$$

9.  $1000 = 2 \times 2 \times 2 \times 5 \times 5 \times 5$

$$56 = 2 \times 2 \times 2 \times 7$$

$$HCF \text{ of } 1000 \text{ and } 56 = 8$$

$\therefore$  Maximum number of columns = 8

10.  $a = 1 \times a$

$$b = 1 \times b$$

$$HCF \text{ of } a \text{ and } b = 1$$

$$\text{Their LCM} = 1 \times a \times b$$

$$LCM \text{ of } a \text{ and } b = ab$$

11. AS  $4025 > 1656$  So applying Euclid's division algorithm on 4025 and 1656 we get

$$4025 = 1656 \times 2 + 713$$

$$1656 = 713 \times 2 + 230$$

$$713 = 230 \times 3 + 23$$

$$230 = 23 \times 10$$

Hence, HCF(1656, 4025) = 23

12. The smallest number divisible by 520 and 468 = LCM(520,468)

Prime factors of 520 and 468 are :

$$520 = 2^3 \times 5 \times 13$$

$$468 = 2 \times 2 \times 3 \times 3 \times 13$$

$$\text{Hence LCM}(520,468) = 2^3 \times 3^2 \times 5 \times 13 = 8 \times 9 \times 5 \times 13 = 4680$$

Now the smallest number which when increased by 17 is exactly divisible by both 520 and 468.

$$= \text{LCM}(520,468)-17$$

$$= 4680-17$$

$$= 4663$$

13. We can write the two given irrational numbers as:

$$(\sqrt{2})^2 = 2 \text{ and } (\sqrt{3})^2 = 3$$

Let p be any rational number between  $\sqrt{2}$  and  $\sqrt{3}$ .

$$\Rightarrow (\sqrt{2})^2 < (p)^2 < (\sqrt{3})^2$$

$$\Rightarrow 2 < (p)^2 < 3$$

One possible value of  $(p)^2 = 2.25$

$$\Rightarrow p = 1.5$$

14. Let p be a prime number and if possible, let  $\sqrt{p}$  be rational.

$$\therefore \sqrt{p} = \frac{m}{n}, \text{ where } m \text{ and } n \text{ are co-primes and } n \neq 0$$

Squaring on both sides, we get

$$\frac{(\sqrt{p})^2}{1} = \left(\frac{m}{n}\right)^2$$

$$\text{or, } p = \frac{m^2}{n^2}$$

$$\text{or, } pn^2 = m^2 \dots\dots\dots(i)$$

$\therefore$  Hence p is a factor of  $m^2$ , So p is a factor of m ..... (1)

So let  $m=pt$ , t is any integer

On putting  $m=pt$  in.(i), we get

$$pn^2 = p^2 t^2$$

$$n^2 = pt^2$$

Hence  $p$  is a factor of  $n^2$ , So  $p$  is a factor of  $n$  ..... (2)

From (1) and (2)  $p$  is a common factor of  $m$  and  $n$

Thus this contradicts the fact that  $m$  and  $n$  are co-primes.

The contradiction arises by assuming that  $\sqrt{p}$  is rational.

Hence,  $\sqrt{p}$  is irrational

15. Given numbers are 180, 252 and 324.

$$324 > 252 > 180$$

On applying Euclid's Division lemma for 324 and 252, we get

$$324 = (252 \times 1) + 72$$

Here, remainder =  $72 \neq 0$

So, again applying Euclid's Division lemma with new dividend 252 and new divisor 72, we get

$$252 = (72 \times 3) + 36$$

Here, remainder =  $36 \neq 0$

So, again applying Euclid's Division lemma with new dividend 72 and new divisor 36, we get

$$72 = (36 \times 2) + 0$$

Here, remainder = 0 and divisor is 36

So, HCF of 324 and 252 is 36

Now, applying Euclid's Division lemma for 180 and 36, we get

$$180 = (36 \times 5) + 0$$

Here, remainder = 0

So HCF of 180 and 36 is 36.

Hence, HCF of 180, 252 and 324 is 36.

16. Suppose  $\sqrt{3} = \frac{a}{b}$ , where  $a$  and  $b$  are co-prime integers,  $b \neq 0$

Squaring both sides,

$$\Rightarrow 3 = \frac{a^2}{b^2}$$

Multiplying with  $b$  on both sides,

$$\Rightarrow 3b = \frac{a^2}{b}$$

**LHS** =  $3 \times b = \text{Integer}$

**RHS** =  $\frac{a^2}{b} = \frac{\text{Integer}}{\text{Integer}} = \text{Rational Number}$

$\Rightarrow \text{LHS} \neq \text{RHS}$

∴ Our supposition is wrong.

⇒  $\sqrt{3}$  is irrational.

Suppose  $15 + 17\sqrt{3}$  is a rational number.

∴  $15 + 17\sqrt{3} = \frac{a}{b}$ , where  $a$  and  $b$  are co-prime,  $b \neq 0$

⇒  $17\sqrt{3} = \frac{a}{b} - 15$

$\sqrt{3} = \frac{a-15b}{17b}$

$\frac{a-15b}{17b}$  is rational number,

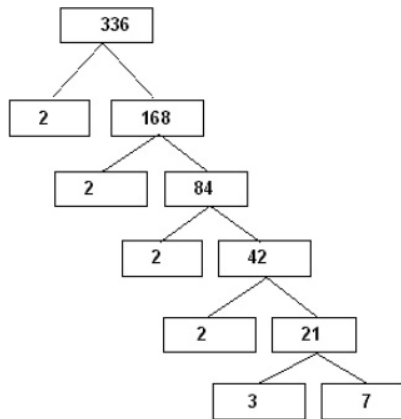
$\sqrt{3}$  is irrational.

∴  $\sqrt{3} \neq \frac{a-15b}{17b}$

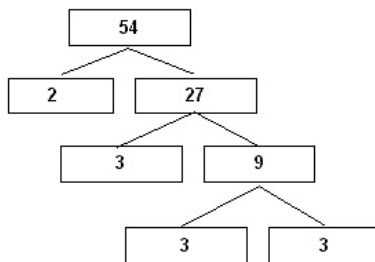
∴ Our supposition is wrong.

⇒  $15 + 17\sqrt{3}$  is irrational.

17.



So,  $336 = 2 \times 2 \times 2 \times 2 \times 3 \times 7 = 2^4 \times 3 \times 7$



So,  $54 = 2 \times 3 \times 3 \times 3 = 2 \times 3^3$

Therefore,

$\text{LCM}(336, 54) = 2^4 \times 3^3 \times 7 = 3024$

$\text{HCM}(336, 54) = 2 \times 3 = 6$ .

Verification:

$\text{LCM} \times \text{HCF} = 3024 \times 6 = 18144$  and  $336 \times 54 = 18144$

i.e.  $\text{LCM} \times \text{HCF} = \text{product of two numbers}$

18. It is given that on dividing the polynomial  $4x^4 - 5x^3 - 39x^2 - 46x - 2$  by the polynomial  $g(x)$ , the quotient is  $x^2 - 3x - 5$  and the remainder is  $-5x + 8$ . We have to find the polynomial  $g(x)$ .

Now, we know that

Dividend = (Divisor  $\times$  Quotient) + Remainder

$$4x^4 - 5x^3 - 39x^2 - 46x - 2 = g(x)(x^2 - 3x - 5) + (-5x + 8)$$

$$\text{or, } 4x^4 - 5x^3 - 39x^2 - 46x - 2 + 5x - 8 = g(x)(x^2 - 3x - 5)$$

$$\text{or, } 4x^4 - 5x^3 - 39x^2 - 41x - 10 = g(x)(x^2 - 3x - 5)$$

$$g(x) = \frac{4x^4 - 5x^3 - 39x^2 - 41x - 10}{(x^2 - 3x - 5)}$$

$$\begin{array}{r} \phantom{x^2 - 3x - 5} \underline{4x^2 + 7x + 2} \\ x^2 - 3x - 5 \overline{) 4x^4 - 5x^3 - 39x^2 - 41x - 10} \\ \underline{4x^4 - 12x^3 - 20x^2} \phantom{- 41x - 10} \\ - \phantom{4x^4} + \phantom{4x^4} \phantom{- 20x^2} \phantom{- 41x - 10} \\ \phantom{4x^4 - 12x^3 - 20x^2} \underline{7x^3 - 19x^2 - 41x - 10} \\ \phantom{4x^4 - 12x^3 - 20x^2} \underline{7x^3 - 21x^2 - 35x} \phantom{- 10} \\ - \phantom{4x^4 - 12x^3 - 20x^2} + \phantom{4x^4 - 12x^3 - 20x^2} \phantom{- 35x} \phantom{- 10} \\ \phantom{4x^4 - 12x^3 - 20x^2} \phantom{7x^3 - 19x^2 - 41x - 10} \underline{2x^2 - 6x - 10} \\ \phantom{4x^4 - 12x^3 - 20x^2} \phantom{7x^3 - 19x^2 - 41x - 10} \underline{2x^2 - 6x - 10} \\ - \phantom{4x^4 - 12x^3 - 20x^2} + \phantom{4x^4 - 12x^3 - 20x^2} \phantom{- 35x} \phantom{- 10} \phantom{- 10} \\ \phantom{4x^4 - 12x^3 - 20x^2} \phantom{7x^3 - 19x^2 - 41x - 10} \phantom{2x^2 - 6x - 10} \underline{0} \end{array}$$

Hence,  $g(x) = 4x^2 + 7x + 2$

19. On applying the Euclid's division lemma to find HCF of 152, 272, we get

$$\begin{array}{r} 152 \overline{) 272} \quad (1 \\ \underline{152} \\ 120 \end{array}$$

$$\begin{array}{r} 120 \overline{) 152} \quad (1 \\ \underline{120} \\ 32 \end{array}$$

$$272 = 152 \times 1 + 120$$

Here the remainder = 0.

Using Euclid's division lemma to find the HCF of 152 and 120, we get

$$152 = 120 \times 1 + 32$$

Again the remainder = 0.

Using division lemma to find the HCF of 120 and 32, we get

$$\begin{array}{r} 32 \overline{)120} \quad (3 \\ \underline{96} \\ 24 \end{array}$$

$$120 = 32 \times 3 + 24$$

Similarly,

$$\begin{array}{r} 8 \overline{)24} \quad (3 \\ \underline{24} \\ 0 \end{array}$$

$$32 = 24 \times 1 + 8$$

$$24 = 8 \times 3 + 0$$

HCF of 272 and 152 is 8.

$272 \times 8 + 152x = \text{H.C.F. of the numbers}$

$$\Rightarrow 8 = 272 \times 8 + 152x$$

$$\Rightarrow 8 - 272 \times 8 = 152x$$

$$\Rightarrow 8(1 - 272) = 152x$$

$$\Rightarrow x = \frac{-2168}{152} = \frac{-271}{19}$$

20. Let  $x = 2p + 1$  and  $y = 2q + 1$

$$\therefore x^2 + y^2 = (2p + 1)^2 + (2q + 1)^2$$

$$= 4p^2 + 4p + 1 + 4q^2 + 4q + 1$$

$$= 4(p^2 + q^2 + p + q) + 2$$

$$= 2(2p^2 + 2q^2 + 2p + 2q + 1)$$

$$= 2m \quad \text{where } m = (2p^2 + 2q^2 + 2p + 2q + 1)$$

$\therefore x^2 + y^2$  is an even number but not divisible by 4.